

# Ornithopter Flight Stabilization

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## ABSTRACT

The quasi-steady aerodynamics model and the vehicle dynamics model of ornithopter flight are explained, and numerical methods are described to capture limit cycle behavior in ornithopter flight. The Floquet method is used to determine stability in forward flight, and a linear discrete-time state-space model is developed. This is used to calculate stabilizing and disturbance-rejecting controllers.

**Keywords:** Ornithopter, Floquet multipliers, Stabilization

## NOMENCLATURE

$\phi$	=	angle of flapping oscillation
$\phi_0$	=	amplitude of flapping oscillation
$\phi_{?0}$	=	amplitude of wing twist at the tip
$\omega$	=	frequency of flapping
$t$	=	time
$r$	=	coordinate along span of a wing
$\tau$	=	instantaneous wing twist
$\phi_0$	=	phase of flapping oscillation
$\phi_{?0}$	=	phase of twisting oscillation
$\Gamma$	=	circulation around the airfoil
$C_L$	=	translational lift coefficient
$C_R$	=	rotational lift coefficient
$c(r)$	=	local chord value
$u$	=	local section velocity parallel to chord
$v$	=	local section velocity normal to chord
$F_v$	=	viscous force
$\rho$	=	air density
$C_D(0)$	=	drag coefficient at zero angle of attack
$C_D(\pi/2)$	=	drag coefficient at 90° angle of attack
$dF_x$	=	local force on the wing parallel to chord
$dF_y$	=	local force on the wing normal to chord
$m_w$	=	wing mass
$m_{11}, m_{22}$	=	added mass parameter
$\alpha$	=	angle of attack
$R$	=	wing length
$\tau$	=	airfoil moment
$U$	=	vehicle forward velocity
$W$	=	vehicle velocity normal to forward velocity
$Q$	=	vehicle pitch rate
$\Phi$	=	vehicle pitch angle
$g$	=	gravitational constant
$F_x$	=	total aerodynamic force on vehicle in forward direction
$F_z$	=	total force on vehicle in downward normal to forward direction
$m$	=	vehicle mass
$I_y$	=	moment of inertia about pitching axis